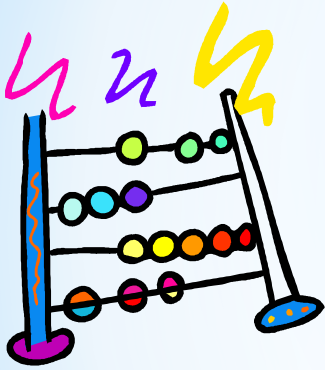


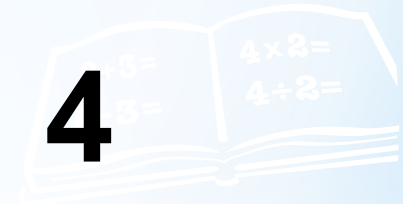


AVANTI HOUSE

EXCELLENCE · VIRTUE · DEVOTION



# Year 3 and 4 Mathematics



## Parent Workshop 2016-17

# Contents



- The new curriculum - what is new in Year 3 and 4.
- 4 operations- including methods used
- Mental Maths
- How you can help at home
- Online support

# What's new?



- Focus on various topics each term
- Increased focus on number
- Roman numerals to 100
- Multiplying fractions
- Less focus on 'statistics'
- Larger numbers

High expectations  
are the key to  
everything.

Sam Walton

# Times tables



By the end of year 4 pupils should:

- Memorise their multiplication tables up to and including the 12 times table
- Show precision and fluency in their work
- Should read and understand mathematical vocabulary correctly and confidently

x	1	2	3	4	5	6	7	8	9	10	11	12
1	1	2	3	4	5	6	7	8	9	10	11	12
2	2	4	6	8	10	12	14	16	18	20	22	24
3	3	6	9	12	15	18	21	24	27	30	33	36
4	4	8	12	16	20	24	28	32	36	40	44	48
5	5	10	15	20	25	30	35	40	45	50	55	60
6	6	12	18	24	30	36	42	48	54	60	66	72
7	7	14	21	28	35	42	49	56	63	70	77	84
8	8	16	24	32	40	48	56	64	72	80	88	96
9	9	18	27	36	45	54	63	72	81	90	99	108
10	10	20	30	40	50	60	70	80	90	100	110	120
11	11	22	33	44	55	66	77	88	99	110	121	132
12	12	24	36	48	60	72	84	96	108	120	132	144

# The Four Operations

## Addition



add more plus  
increase total  
sum altogether

teaching ideas

## Subtraction



subtract minus  
less take away  
decrease leave  
fewer difference

teaching ideas

## Multiplication



multiply lots of  
times groups of  
multiplied by array  
repeated product  
addition

teaching ideas

## Division



divide remainder  
share share equally  
groups of divided by  
repeated each  
subtraction

teaching ideas

# Adding

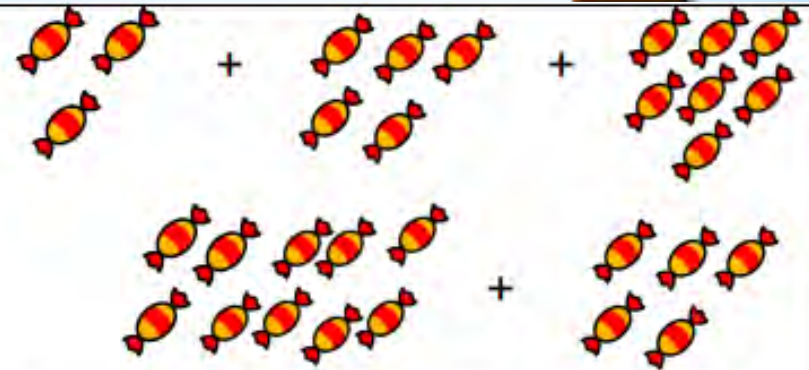


## Adding three single digits

$4 + 7 + 6 = 17$   
Put 4 and 6 together to make 10. Add on 7.



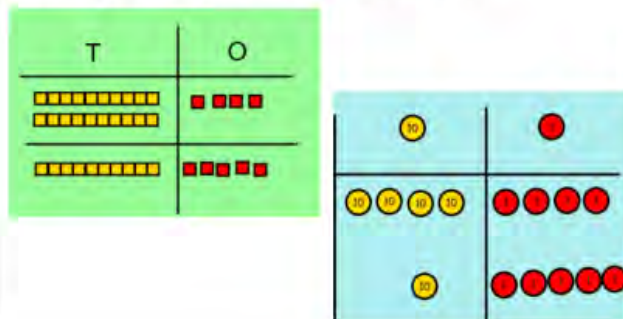
Following on from making 10, make 10 with 2 of the digits (if possible) then add on the third digit.



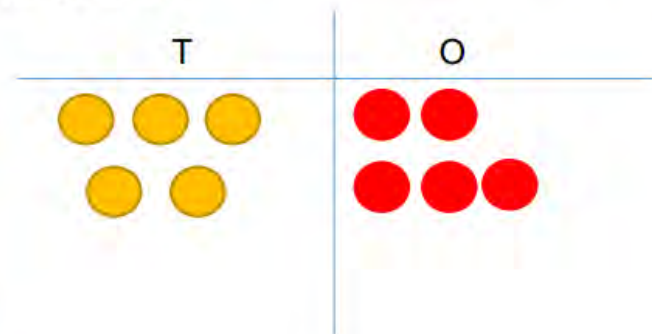
Add together three groups of objects. Draw a picture to recombine the groups to make 10.

## Column method- no regrouping

$24 + 15 =$   
Add together the ones first then add the tens. Use the Base 10 blocks first before moving onto place value counters.



After practically using the base 10 blocks and place value counters, children can draw the counters to help them to solve additions.

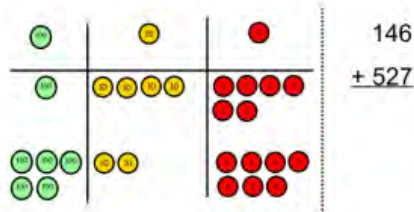


# Adding

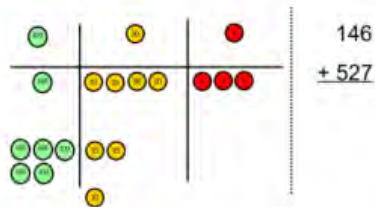


## Column method- regrouping

Make both numbers on a place value grid.



Add up the units and exchange 10 ones for one 10.

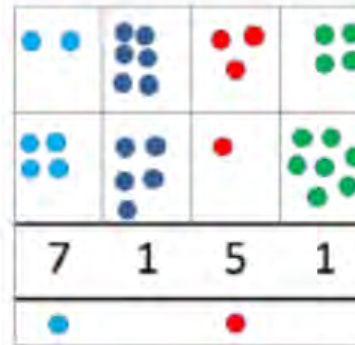


Add up the rest of the columns, exchanging the 10 counters from one column for the next place value column until every column has been added.

This can also be done with Base 10 to help children clearly see that 10 ones equal 1 ten and 10 tens equal 100.

As children move on to decimals, money and decimal place value counters can be used to support learning.

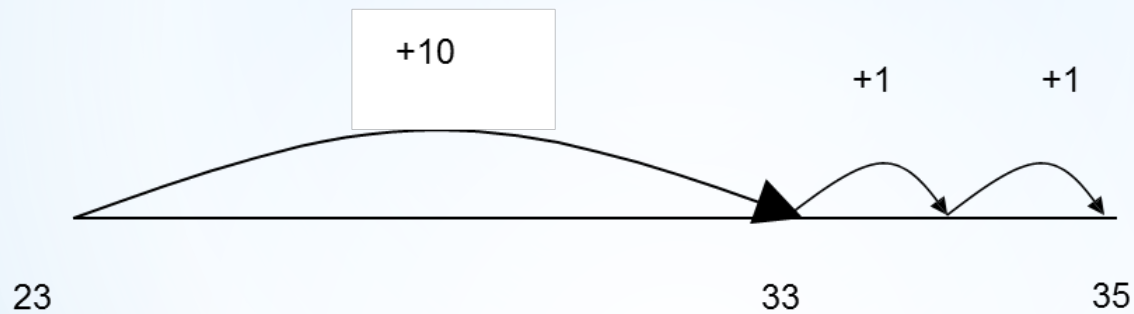
Children can draw a pictorial representation of the columns and place value counters to further support their learning and understanding.



# Adding



$$12 + 23 =$$



$$\begin{array}{r} 23 + 12 \\ \diagdown \quad \diagup \\ 20 + 10 + 3 + 2 = 30 + 5 = 35 \end{array}$$

Expanded method  
**Partitioning**



# Adding



$$83 + 42 = 125$$

$$\begin{array}{r} 80 + 3 \\ + 40 + 2 \\ \hline 120 + 5 \end{array}$$

move to

$$\begin{array}{r} 83 \\ + \underline{42} \\ 5 \\ \underline{120} \\ 125 \end{array}$$

# Adding



$$\begin{array}{r} 358 \\ + 73 \\ \hline 431 \\ \hline \end{array}$$

1 1



Carrying over must be done put underneath

So in any class, the same example might be given, but children work it out in different ways, according to their level of understanding.

# Adding



Choose a method you are unfamiliar with to solve these sums.

1.  $73 + 57$

2.  $153 + 89$

3.  $163 + 144$

4.  $287 + 193$

# Subtracting



## Counting back

Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones.

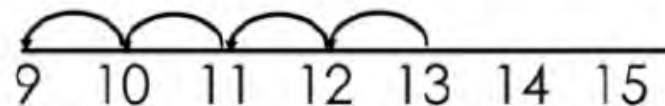


$$13 - 4$$

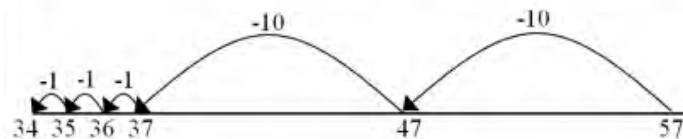
Use counters and move them away from the group as you take them away counting backwards as you go.



Count back on a number line or number track



Start at the bigger number and count back the smaller number showing the jumps on the number line.

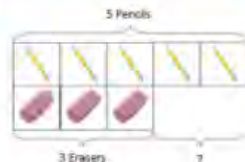


## Find the difference

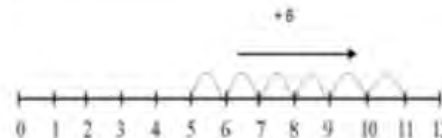
Compare amounts and objects to find the difference.



Use cubes to build towers or make bars to find the difference



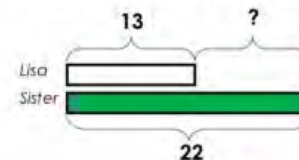
Use basic bar models with items to find the difference



Count on to find the difference.

### Comparison Bar Models

Lisa is 13 years old. Her sister is 22 years old. Find the difference in age between them.

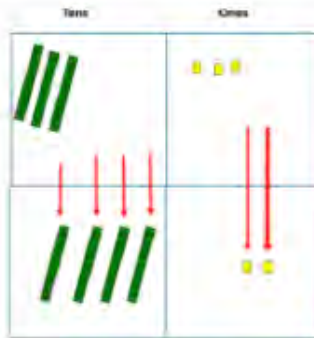


VO

# Subtracting

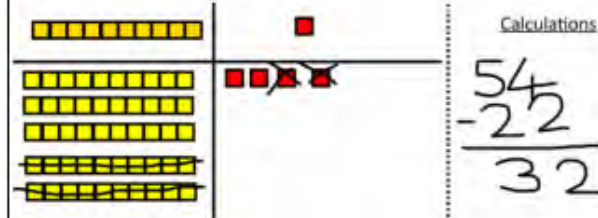


Column method without regrouping



Use Base 10 to make the bigger number then take the smaller number away.

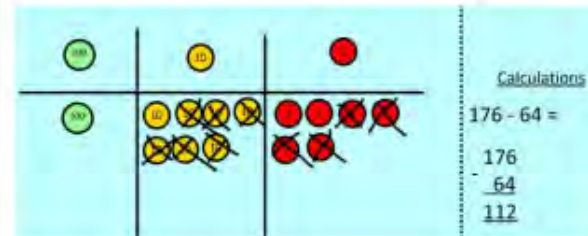
Show how you partition numbers to subtract. Again make the larger number first.



Calculations

$$\begin{array}{r} 54 \\ - 22 \\ \hline 32 \end{array}$$

Draw the Base 10 or place value counters alongside the written calculation to help to show working.



Calculations

$$\begin{array}{r} 176 \\ - 64 \\ \hline 112 \end{array}$$

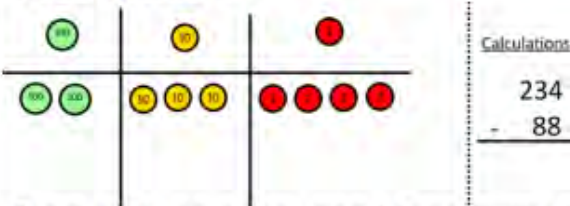
# Subtracting



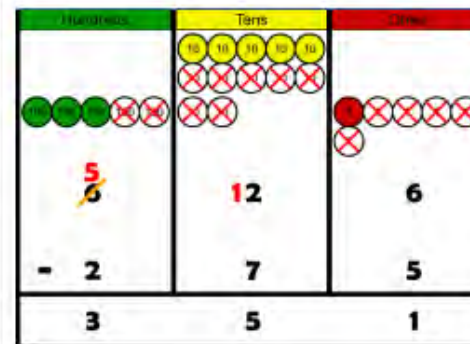
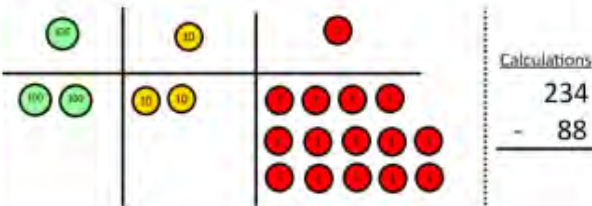
## Column method with regrouping

Use Base 10 to start with before moving on to place value counters. Start with one exchange before moving onto subtractions with 2 exchanges.

Make the larger number with the place value counters



Start with the ones, can I take away 8 from 4 easily? I need to exchange one of my tens for ten ones.



Draw the counters onto a place value grid and show what you have taken away by crossing the counters out as well as clearly showing the exchanges you make.



When confident, children can find their own way to record the exchange/regrouping.

Just writing the numbers as shown here shows that the child understands the method and knows when to exchange/regroup.

# Subtracting



$$37 - 12$$

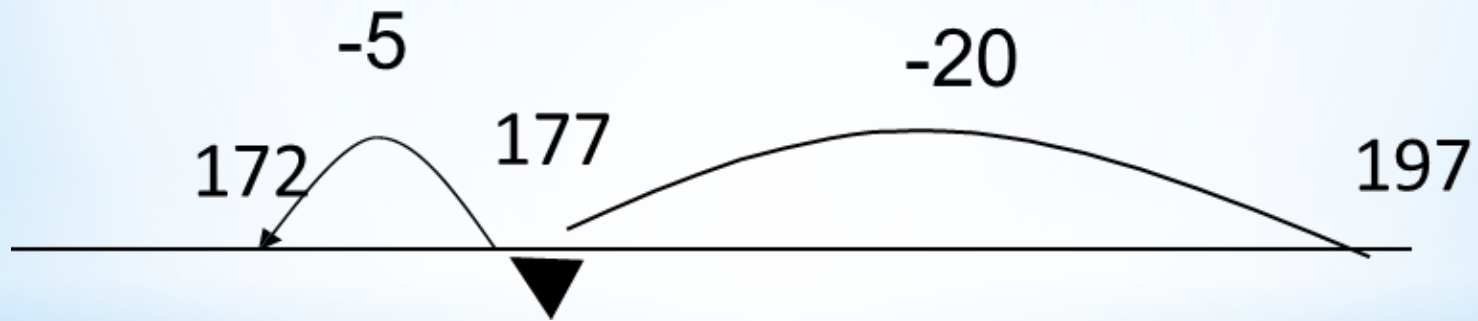


$$\begin{aligned} 37 - 12 &= 37 - 10 - 2 \\ &= 27 - 2 \\ &= 25 \end{aligned}$$

# Subtracting



$$197 - 25 = 172$$





# Subtracting



$$98 - 24 = 74$$

$$\begin{array}{r} 90 + 8 \\ - 20 + 4 \\ \hline 70 + 4 \end{array}$$

# Subtracting

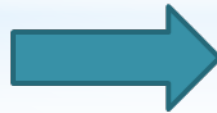


$$\begin{array}{r} \phantom{9}^8 \phantom{2}^1 \\ \cancel{9} \phantom{2} \\ - \underline{38} \\ 54 \end{array}$$

Expanded method

$$902 - 38 = 864$$

$$\begin{array}{r} 900 + 0 + 2 \\ - \phantom{900} \phantom{+ 0} \phantom{+ 2} \\ \phantom{900} \phantom{+ 0} \phantom{+ 2} \\ \underline{\phantom{900} \phantom{+ 0} \phantom{+ 2}} \phantom{+ 8} \\ \phantom{900} \phantom{+ 0} \phantom{+ 2} \phantom{+ 8} \end{array}$$



$$\begin{array}{r} 800 + 90 + 12 \\ - \phantom{800} \phantom{+ 90} \phantom{+ 12} \\ \phantom{800} \phantom{+ 90} \phantom{+ 12} \\ \underline{\phantom{800} \phantom{+ 90} \phantom{+ 12}} \phantom{+ 8} \\ 800 + 60 + 4 \end{array}$$

# Subtracting



Choose a method you are unfamiliar with to solve these calculations.

1.  $97 - 42$

2.  $183 - 55$

3.  $188 - 54$

4.  $394 - 131$

5.  $73 - 29$

6.  $194 - 38$

# Multiplying



## Repeated addition

Use different objects to add equal groups.

There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there?

2 add 2 add 2 equals 6

$5 + 5 + 5 = 15$

Write addition sentences to describe objects and pictures.

$2 + 2 + 2 + 2 + 2 = 10$

## Arrays- showing commutative multiplication

Create arrays using counters/ cubes to show multiplication sentences.

Draw arrays in different rotations to find **commutative** multiplication sentences.

Link arrays to area of rectangles.

Use an array to write multiplication sentences and reinforce repeated addition.

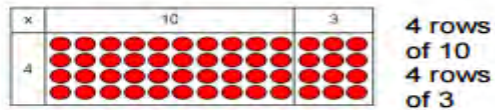
$5 + 5 + 5 = 15$   
 $3 + 3 + 3 + 3 + 3 = 15$   
 $5 \times 3 = 15$   
 $3 \times 5 = 15$

# Multiplying



## Grid Method

Show the link with arrays to first introduce the grid method.



Move on to using Base 10 to move towards a more compact method.



Move on to place value counters to show how we are finding groups of a number. We are multiplying by 4 so we need 4 rows.



Fill each row with 126.



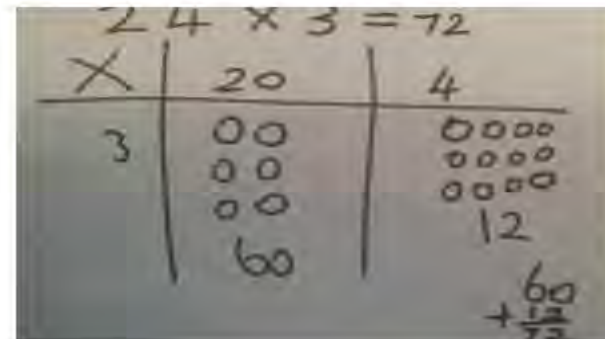
Add up each column, starting with the ones making any exchanges needed.



Then you have your answer.

Children can represent the work they have done with place value counters in a way that they understand.

They can draw the counters, using colours to show different amounts or just use circles in the different columns to show their thinking as shown below.

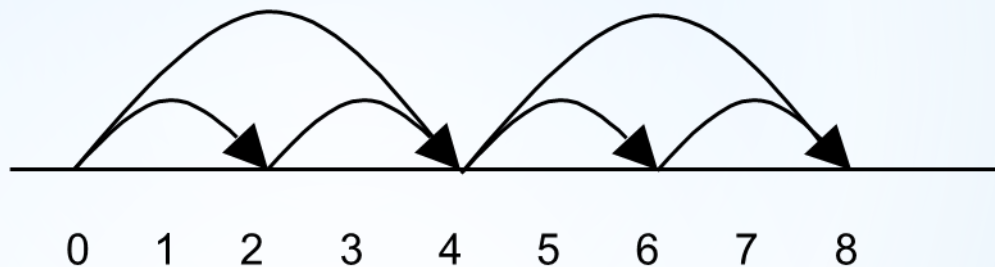


# Multiplying



repeated addition:

$$2 + 2 + 2 + 2$$



Grid method or partitioning  
 $35 \times 2 = 70$

x	30	5
2	60	10

$$60 + 10 = 70$$

# Multiplying



$$23 \times 7 = 161$$

	T		U
	20		3
x			
7	140		21

$$140 + 21 = 161$$

This method is extended to multiplying a 3 digit number by a single digit

# Multiplying



Still use the grid method to multiply numbers up to 3 digits by a single digit.

Move onto more formal method when appropriate:

Children could record in brackets – e.g. 15 (3 X 5)

Similar to grid method but using vertical recording.

$$125 \times 3$$

$$\begin{array}{r} 125X \\ \underline{\quad 3} \\ 15 \\ 60 \\ \underline{300} \\ \underline{375} \end{array}$$



$$\begin{array}{r} 125 \times \\ \underline{\quad 3} \\ \underline{375} \end{array}$$



# Multiplying



Choose a method you are unfamiliar to solve these calculations.

1.  $89 \times 5$

2.  $274 \times 8$

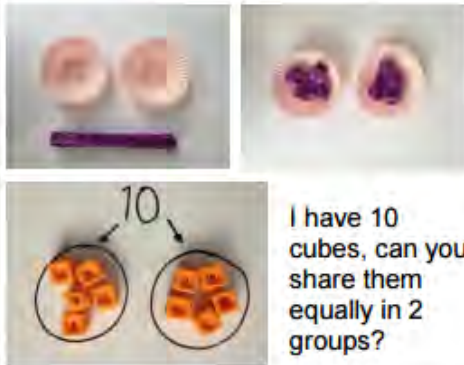
3.  $285 \times 4$

4.  $317 \times 7$

# Dividing

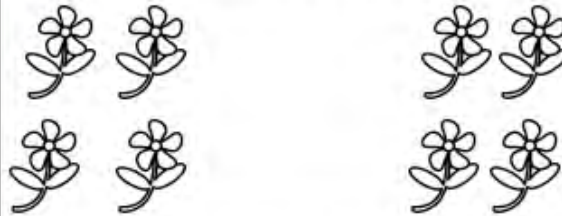


## Sharing objects into groups



I have 10 cubes, can you share them equally in 2 groups?

Children use pictures or shapes to share quantities.



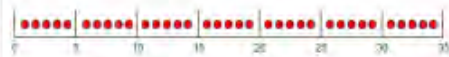
$$8 \div 2 = 4$$

Share 9 buns between three people.

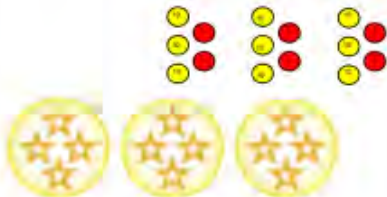
$$9 \div 3 = 3$$

## Division as grouping

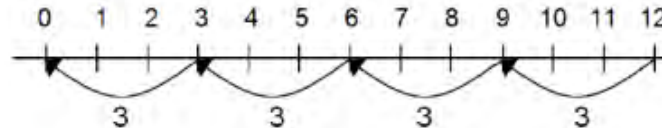
Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.



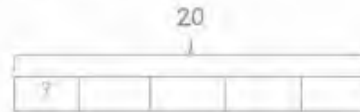
$$96 \div 3 = 32$$



Use a number line to show jumps in groups. The number of jumps equals the number of groups.



Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group.



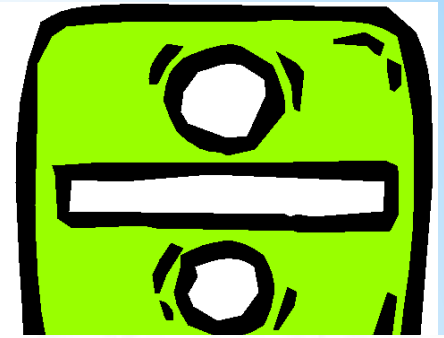
$$20 \div 5 = ?$$

$$5 \times ? = 20$$

$$28 \div 7 = 4$$

Divide 28 into 7 groups. How many are in each group?

# Dividing



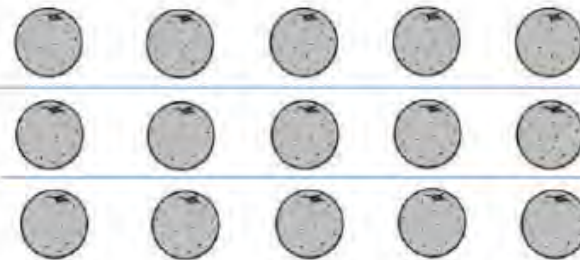
## Division within arrays



Link division to multiplication by creating an array and thinking about the

number sentences that can be created.

Eg  $15 \div 3 = 5$      $5 \times 3 = 15$   
 $15 \div 5 = 3$      $3 \times 5 = 15$



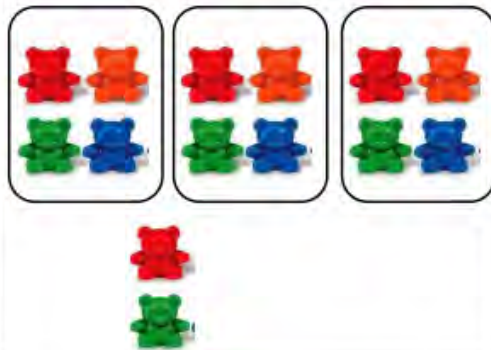
Draw an array and use lines to split the array into groups to make multiplication and division sentences.

Find the inverse of multiplication and division sentences by creating four linking number sentences.

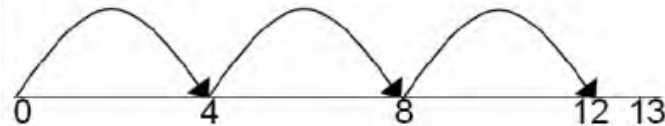
$7 \times 4 = 28$   
 $4 \times 7 = 28$   
 $28 \div 7 = 4$   
 $28 \div 4 = 7$

## Division with a remainder

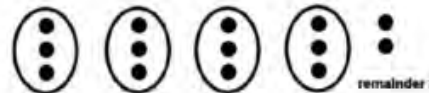
$14 \div 3 =$   
 Divide objects between groups and see how much is left over



Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder.



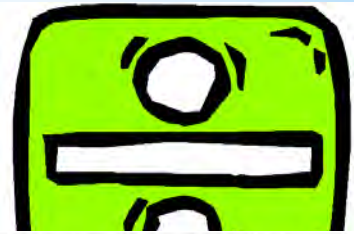
Draw dots and group them to divide an amount and clearly show a remainder.



Complete written divisions and show the remainder using r.

$29 \div 8 = 3 \text{ REMAINDER } 5$   
↑    ↑    ↑                    ↑  
dividend   divisor   quotient                    remainder

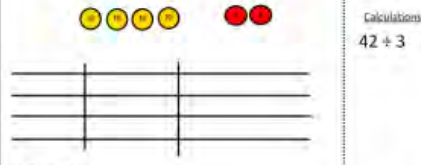
# Dividing



## Short division

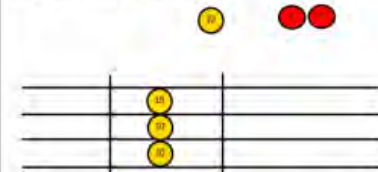


Use place value counters to divide using the bus stop method alongside



$$42 \div 3 =$$

Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over.

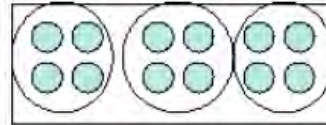


We exchange this ten for ten ones and then share the ones equally among the groups.



We look how much in 1 group so the answer is 14.

Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups.



Encourage them to move towards counting in multiples to divide more efficiently.

Begin with divisions that divide equally with no remainder.

$$\begin{array}{r} 218 \\ 3 \overline{) 4872} \end{array}$$

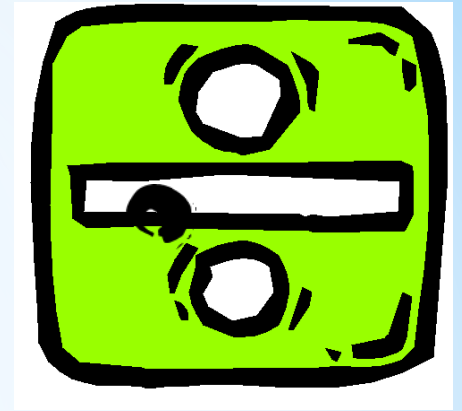
Move onto divisions with a remainder.

$$\begin{array}{r} 86 \text{ r } 2 \\ 5 \overline{) 432} \end{array}$$

Finally move into decimal places to divide the total accurately.

$$\begin{array}{r} 14.6 \\ 35 \overline{) 511.0} \end{array}$$

# Dividing

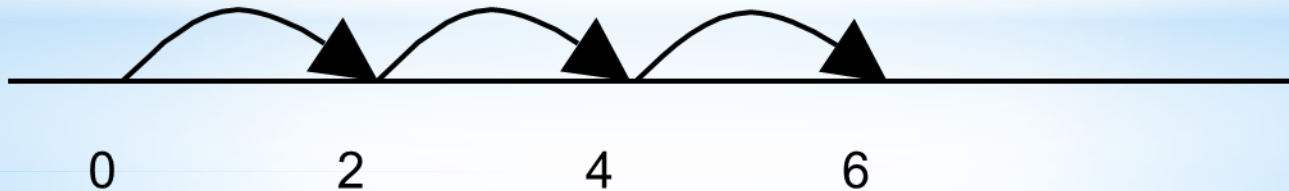


$$6 \div 2 = 3$$

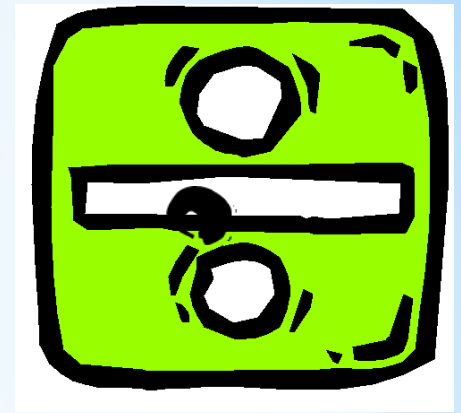
**Sharing** – 6 sweets are shared between 2 people. How many do they have each?



**Grouping** – There are 6 sweets. How many people can have 2 each? (How many 2's make 6?)



# Dividing



With more advanced numbers, e.g.  
dividing by 3 or 4

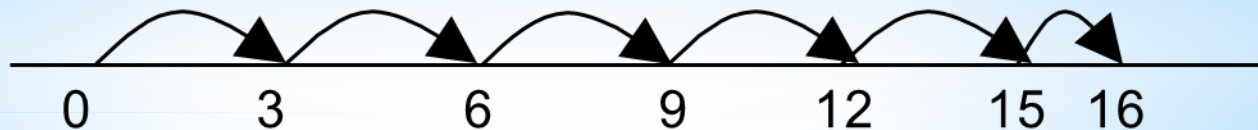
*Remainders*

$$16 \div 3 = 5 \text{ r}1$$

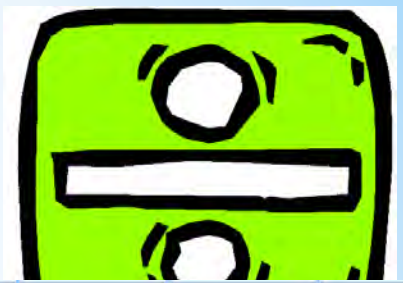
Sharing - 16 shared between 3, how many  
left over?

Grouping - How many 3's make 16, how  
many leftover?

e.g.



# Dividing



$$72 \div 3 = 24$$

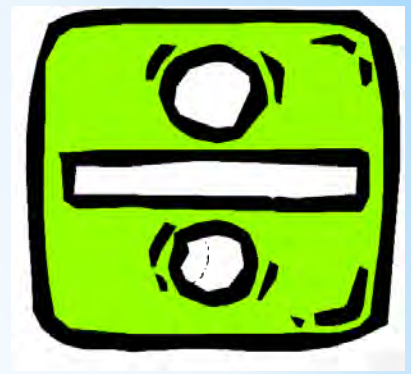
$$\begin{array}{r} 24 \\ 3 \overline{) 72} \\ \underline{60} \\ 12 \\ \underline{12} \\ 0 \end{array}$$

$$20 + 4 = 24$$

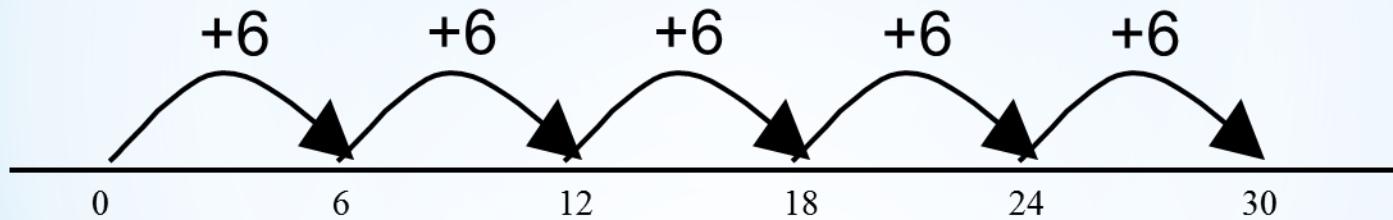
(20 x 3)

+  
(4 x 3)

# Dividing

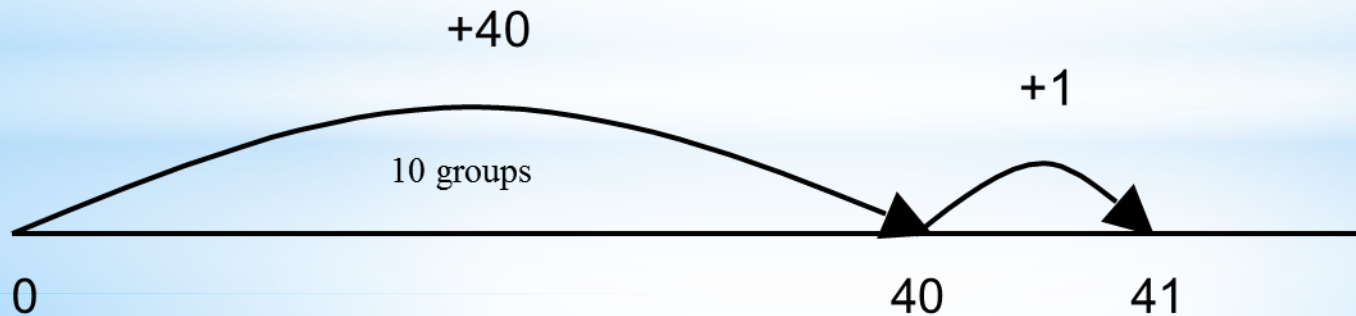


$$30 \div 6 = 5$$



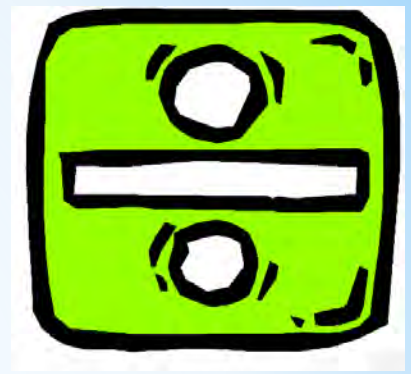
$$41 \div 4 = 10 \text{ r } 1$$

$$\text{or } 41 = (10 \times 4) + 1$$





# Dividing

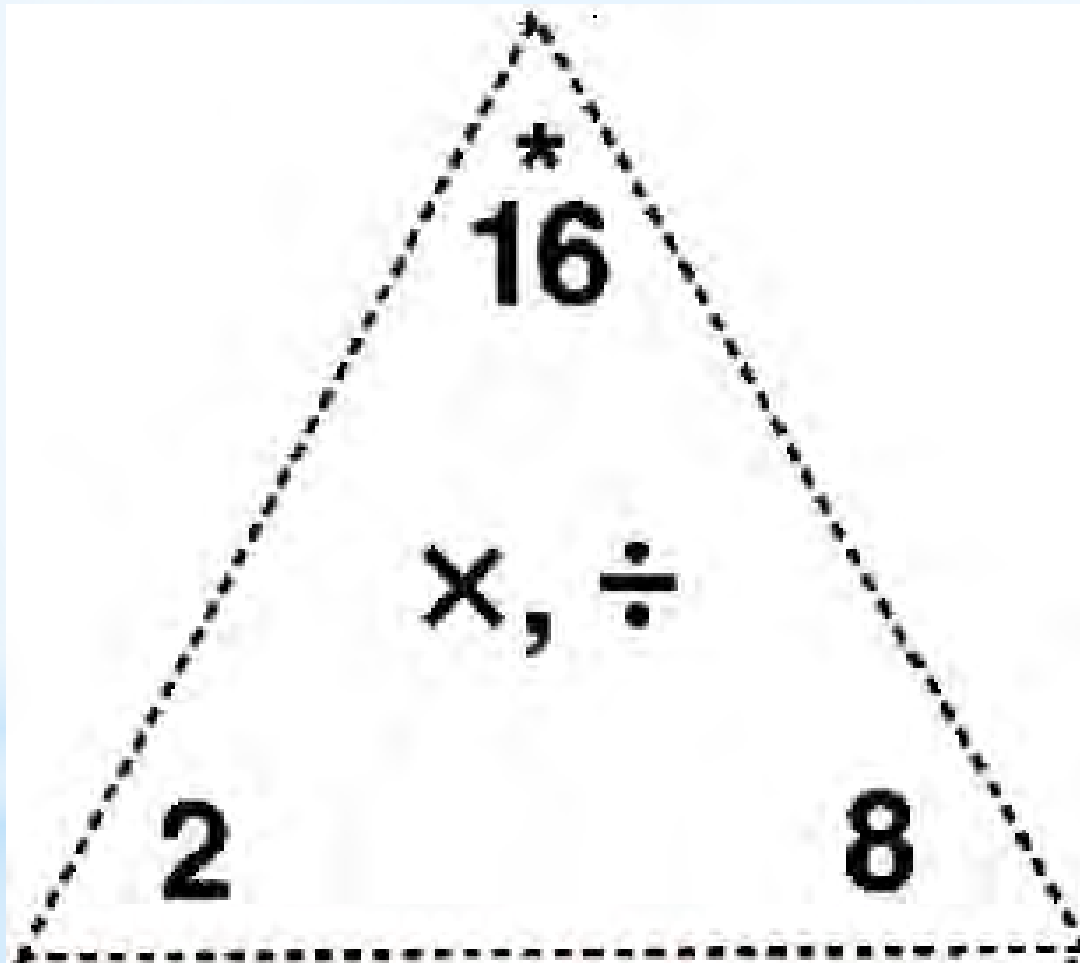
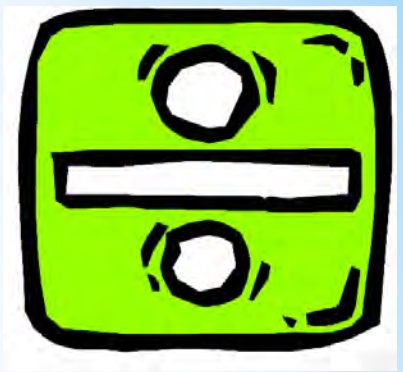


Use 'bus stop' method for division:  
Estimate and check.

$360 \div 8$  is approximately  $400 \div 8 = 50$

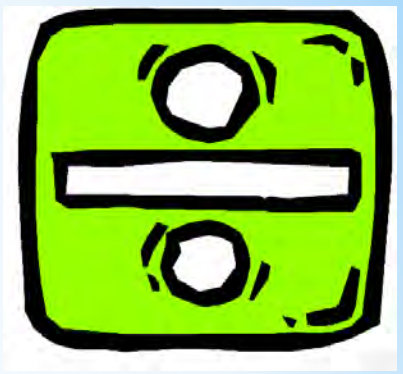
$$\begin{array}{r} 45 \\ 8 \overline{) 360} \end{array}$$

# Dividing



Multiplication and Division Fact Triangle

# Dividing



Have a go at these:

$$\begin{array}{r} 35 \\ \times \div \\ 7 \quad 5 \end{array}$$

$$\begin{array}{r} 45 \\ \times \div \\ 9 \quad 5 \end{array}$$

$$\begin{array}{r} 40 \\ \times \div \\ 8 \quad 5 \end{array}$$

## Dividing

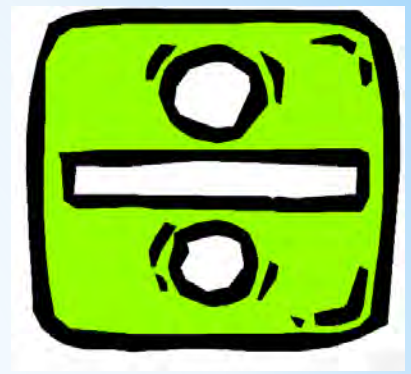
Choose a method you are unfamiliar to solve these calculations.

1.  $35 \div 5$

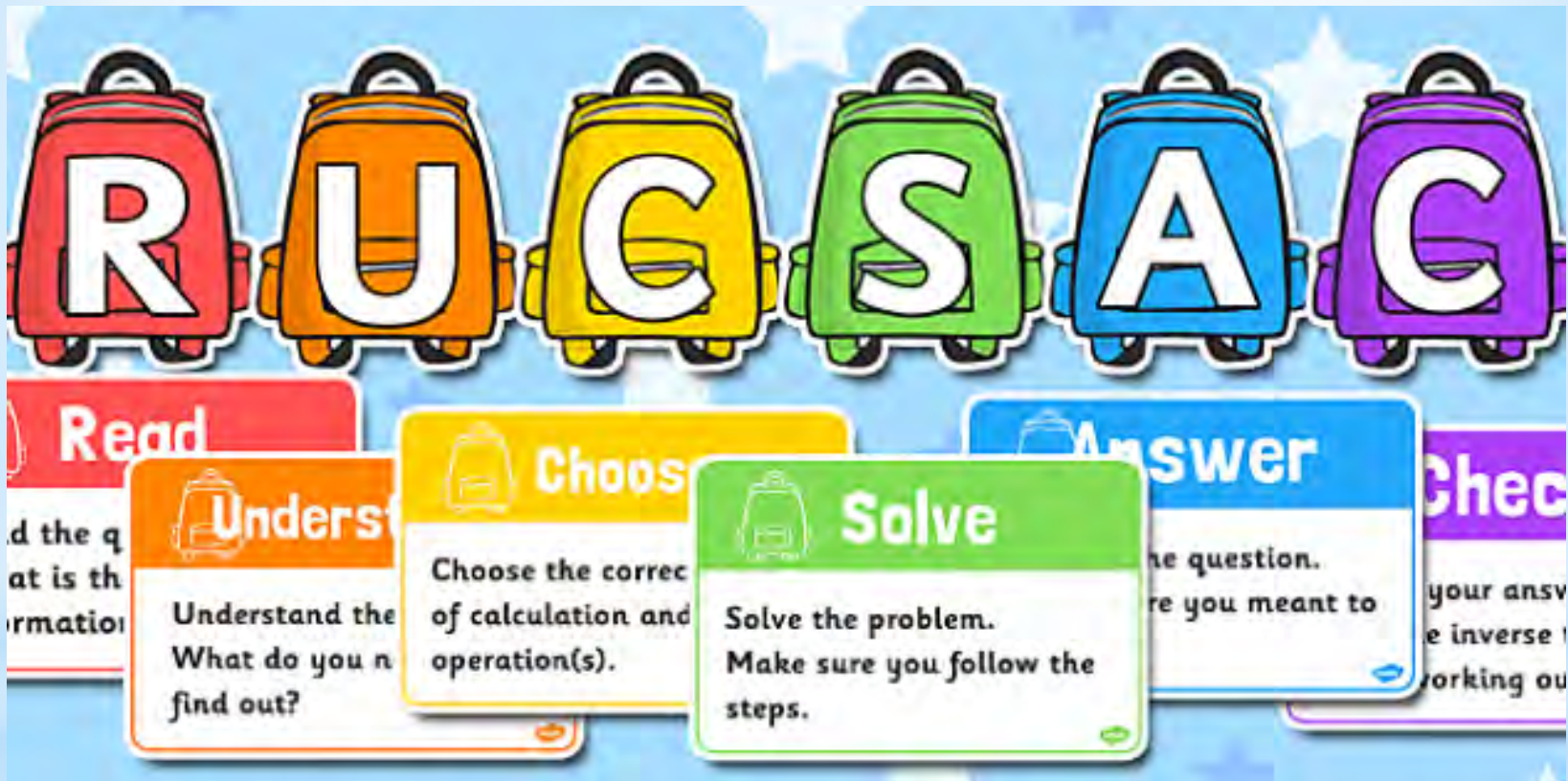
2.  $67 \div 8$

3.  $270 \div 3$

4.  $348 \div 4$



# Word Problems



# Mental Mathematics

## Mental Maths Strategies:

- Use number bonds to 10, 20 and 100
- Use doubles and near doubles
- Counting on and backward in ones, twos, fives, tens
- Partition into tens and units
- Put the biggest number first
- Add 10 then add 1 = adding 11
- Add 10 then subtract 1 = adding 9
- Subtract 10 then subtract 1 = subtracting 11
- Subtract 10 then add 1 = subtracting 9

# How can you help at home?

- Lots of practice – in the car, online games, counting stairs, cars, trees etc
- Playing games – cards, snakes and ladders, dominoes
- Cooking
- Telling the time
- Online Applications

# Online Applications



Multi player  
mental  
maths game



Math Bingo: Four  
operation bingo



Numberjacks:  
Addition facts up  
to 10



Four operation practice



Squeebles Times  
Tables 2



Amazing coin: Learn  
about different British  
currency